## **DEPARTMENT OF MATHEMATICS**

## **COURSE CURRICULUM & MARKING SCHEME**

# B.Sc. PART – II & III MATHEMATICS

**SESSION: 2022-23** 



ESTD: 1958

## GOVT. V.Y.T. PG AUTONOMOUS COLLEGE, DURG, 491001 (C.G.)

(Former Name - Govt. Arts & Science College, Durg)

NAAC Accredited Grade A<sup>+</sup>, College with CPE - Phase III (UGC), STAR COLLEGE (DBT)

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## DEPARTMENT OF MATHEMATICS GOVT. V.Y. T. PG. AUTONOMOUS COLLEGE DURG SYLLABUS

for

#### B.Sc. Part-II

The syllabus with the paper combinations and Marking Scheme for Session 2022-2023.

Paper No. Title of the Paper	Title of the Paper	Marks Allotted in Theory	
	Max	Min	
I	Advanced Calculus	50	
II	Differential Equation	50	
III	Mechanics	50	
	Total	150	50

**Total Marks** 

- 150

The syllabus for **B.Sc. Part-II** is hereby approved by the members of Board of Studies for the session **2022-2023**.

In case, any change or modification is prescribed by Central Board of Studies or Higher Education Deptt., Govt. of Chhattisgarh with respect to content or distribution of marks for Undergraduate syllabi, it will be implemented accordingly.

#### Name & Signature

Chairperson / H.O.D - Dr. M.A. Siddiqui Faculty members Subject Expert -Dr. Madhu Srivastava Dr. Padmavati Subject Expert Dr. Shabnam Khan Dr. Rakesh Tiwari Subject Expert -Dr. S. K. Bhatt Dr. (Smt.) Prachi Singh Representative Members -Dr. Shobha Rani (1) Dr. Anil Kashyap -(2) Shri A. K. Pandey -(3) Dr. Mayur Puri Goswami -

### B.Sc. Part -II (MATHEMATICS) 2022-2023

#### PAPER-I

#### **Advanced Calculus**

Max Marks 50

Course Title	B. Sc. Part – II, Advanced Calculus  Course Outcomes - This course will enable the student to :	
CO No.		
CO No. – 1	Analyze concept of convergence of sequence, series and their various properties.	
CO No 2	Remember about continuity, sequential continuity, uniform continuity.	
CO No 3	Apply the mean value theorem and its geometrical Property, partial differentiation in obtaining envelops and evaluates of given family of curves	
CO No 4	Understand function of several variables and its partial derivatives, Beta Gamma function and its applications.	

- UNIT-I Definition of a sequence. Theorems on limits of sequences. Bounded and Monotonic Sequences, Cauchy's convergence criterion. Series of non-negative terms. comparison tests, Cauchy's integral test, ratio tests, Raabe's, logarithmic, De Morgan and Bertrand's tests (without proof). Alternating series. Leibnitz's theorem. Absolute and conditional convergence.
- UNIT-II Continuity, sequential continuity, properties of continuous functions, uniform continuity.
  Chain rule of differentiability. Mean value theorems and their geometrical interpretations.
  Darboux's intermediate value theorem for derivatives. Taylor's theorem with various forms of Remainders.
- **UNIT-III** Limit and continuity of functions of two variables. Partial differentiation. Change of variables. Euler's theorem on homogeneous functions, Taylor's theorem for functions of two variables, Jacobians.
- UNIT-IV Envelopes. Evolutes. Maxima- Minima and saddle points of functions of two variables. Lagrange's multiplier method.
- **UNIT-V** Beta and Gamma functions. Double and triple integrals, Dirichlet's integrals. Change of order of integration in double integrals.

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#### REFERENCES:

- 1. Gabriel Klaumber, Mathematical Analysis, Marcel Dekkar, Inc. New York, 1975.
- 2. T.M. Apostol, Mathematical analysis, Narosa Publishing House, New Delhi, 1985.
- 3. R.R. Goldberg, Real Analysis, Oxford & I.B.H. Publishing Co., New Delhi,
- 4. D. Soma Sundaram and B. Choudhary, a. first course in Mathematical analysis, Narosa Publishing House, New Delhi, 1997.
- 5. P.K. Jain and S.K. Kaushik, An introduction to Real Analysis, S.Chand & Co., New Delhi, 2000.
- 6. Gorakh Prasad, Differential Calculus, Pothishala Pvt. Ltd., Allahabad.
- 7. Murry R. Spiegel, Theory and Problems of Advanced Calculus, Schaum Publishing Co., New York.
- 8. Gorakh Prasad, Integral Calculus, Pothishala Pvt. Ltd., Allahabad.
- 9. S.C. Malik, Mathematical analysis, Wiley Eastern Ltd., New Delhi.
- 10. O.E. Stanaitis, an Introduction to Sequences, Series and Improper Integrals, Holden Day, Inc., san Francisco, California.
- 11. Earl D. Rainville, Infinite Series, The Macmillan Company, New York.
- 12. Chandrika Prasad, Text Book on algebra and Theory of Equations, Pothishala Pvt. Ltd., Allahabad.
- 13. N. Piskunov, differential and Integral Calculus, Peace Publishers, Moscow.
- 14. Shanti Narayan, A course of Mathematical Analysis, S. Chand and Company, New Delhi.

Subject Expert - Dr. Madhu Srivastava

Subject Expert - Dr. Shabnam Khan

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Subject Expert - Dr. S. K. Bhatt

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(6) Dr. Mayur Puri Goswami -

Dr. Rakesh Tiwari

Dr. Padmavati

Faculty members

Dr. (Smt.) Prachi Singh

#### **B.Sc. Part -II (MATHEMATICS)** 2022-2023

#### PAPER - II

#### DIFFERENTIAL EQUATIONS

Max.Marks.50

Course Title B. Sc. Part – II, Differential Equation	
CO No.	Course Outcomes - This course will enable the student to :
CO No. – 1	Remember Laplace Transformation of derivatives and integral, solution of integrals and system of differential equations.
CO No. – 2	Evaluatepartial differential equations and its various type, Charpits general method of solutions, Partial differential equation of second and higher order, Homogeneous and nonhomogeneous equation with constant coefficient, Mobious method.
CO No 3	Analyze Series solution of differential equation, series method Bessels and Legendrs function with their properties, Orthogonality of functions, Legendre polynomial etc.
CO No 4	Apply Variational problem with fixed boundary, Eular equation for functionals containing first order derivatives, variational problem with moving boundaries, variational principle of least action.

- UNIT-I Laplace Transformation Linearity of the Laplace transformation. Existence theorem for Laplace transforms. Laplace transforms of derivatives and integrals. Shifting theorems. Differentiation and integration of transforms. Convolution theorem. Solution of integral equations and systems of differential equations using the Laplace transformation.
- **UNIT-II** Partial differential equations of the first order. Lagrange's solution. Some special types of equation which can be solved easily by methods other than the general method. Charpit's general method of solution.
- UNIT-III Partial differential equations of second and higher orders. Classification of linear partial differential equations of second order. Homogeneous and non-homogeneous equations with constant coefficients. Partial differential equations reducible to equations with constant coefficients, Monge's methods...
- UNIT-IV Series solutions of differential equations Power series method. Bessel's and Legendre functions and their properties. Convergence, recurrence and generating relations. Orthogonality of functions, Sturm-Liouville problem. Orthogonality of eigen-functions. Reality of eigenvalues. Orthogonality of Bessel's functions and Legendre polynomials.
- UNIT-V Calculus of variations – Variational problems with fixed boundaries - Euler's equation for

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Functional containing first order derivative and one independent variable. Externals. Functionals dependent on higher order derivatives. Funcationals dependent on more than one independent variable. Variational problems in parametric form. Invariance of Eulers Equation under coordinates transformation. Variational problems with moving Boundaries –Functionals dependent on one and two functions. One sided variations. Sufficient conditions for an Extremum – Jacobi and Legendre conditions. Second Variation. Variational principal of least action.

#### REFERENCE

- 1. Erwin Kreyszig, Advanced Engineering Mathematics, John Wiley & sons, Inc. New York, 1999.
- 2. D.A. Murray, Introductory Course on differential Equations, Orient Longman, (India) 1967.
- 3. A.R. Forsyth, a. Treatise on differential Equations, Macmillan and Co.Ltd. London .Lan N. Sneddon, elements of paprtial Differential Equations, McGraw-Hill Book Company, 1988.
- 4. Francis B.Hilderbrand, Advanced Calculus for Applications, Prentic Hall India Pvt.Ltd., New Delhi, 1977.
- 5. Jane Cronin, differential equations, Marcel dekkar, 1994.
- 6. Frank ayres, Theory and Problems of differential Equations, McGraw- Hill Book company, 1972.
- 7. Richard Bronson, Theory and Problems of Differential Equations, McGraw-Hill Inc., 1972.
- 8. A.S. Gupta, Calculus of variations with-applications, Prentice-Hall of India, 1997.
- 9. R. courant and D. Hilbert, Methods of Mathematical Physics, volts. I & II, wiley-Inter science, 1953.
- 10. I.M. Gelfand and s.V. Fomin, calculus of Variations, Prentice-Hill, Englewood Cliffs New Jersey), 1953.
- 11. A.M. Arthurs, Complementary Variational Principles, Calrendon Press, Oxford, 1970.
- 12. V. Kornkov, Variational Principales of Continuum Mechanies with Engineering Applications, vol. I, Rediel Pub.: dordrecht, Holland, 1985.
- 13. T. Oden and J.N. Reddy, Variational Methods in Theoretical Mechanics, Springer-Verlag, 1976.

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**Faculty members** 

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Dr. Rakesh Tiwari

Dr. (Smt.) Prachi Singh



## **B.Sc. Part -II (MATHEMATICS)** 2022-2023 PAPER - III

#### **MECHANICS**

Max.Marks.50

Course Title	B. Sc. Part – II, Machanies
CO No.	Course Outcomes - This course will enable the student to :
CO No. – 1	Analyze Various analytic condition of equilibrium principle of virtual work, catenary.
CO No 2	Remember Forces in three dimensional, Poinsot central axis with problem, null lines and planes.
CO No 3	Apply Simple harmonic motion, Velocity and Acceleration along radial and crossradial direction, problem on central orbits.
CO No 4	Understand Kaplers Law, Motion on smooth and rough plane curves, Resisting medium, Motion of particle of vary mass, acceleration in terms of differentco-ordinates.

#### STATICS:

- **UNIT I** Analytical conditions of equilibrium. Virtual work. Catenary.
- UNIT -II Forces in three dimensions. Poinsot's central axis. Null lines and planes.

#### **DYNAMICS:**

- UNIT-III Simple harmonic motion. Velocities and accelerations along radial and transverse directions. Projectile.
- UNIT-IV Central orbits. Kepler's laws of motion. Velocities and acceleration in tangential and normal directions. Motion on smooth and rough plane curves.
- **UNIT-V** Motion in a resisting medium. Motion of particles of varying mass. Motion of a particle three dimensions. Acceleration in terms of different co-ordinate systems.

#### REFERENCE:

- 1 S.L. Loney, Statics, Macmillan and Company; London Press, 1956.
- 2 R.S. Verma, a Text Book on Statics, Pothishala Pvt. Ltd., Allahabad.

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3 S.L. Loney, An elementary Treatise on the Dynamics of a particle and of rigid bodies . Cambridge University.

#### Name & Signature

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Dr. Rakesh Tiwari

Dr. (Smt.) Prachi Singh -

## DEPARTMENT OF MATHEMATICS GOVT. V.Y. T. PG. AUTONOMOUS COLLEGE, DURG SYLLABUS

for

#### **B.Sc. Part-III**

The syllabus with the paper combinations and Marking Scheme for Session 2022-23.

Paper No.	Title of the Paper	Marks Allotted in Theory	
		Max	Min
I	Analysis	50	
II	Abstract Algebra	50	
III	Optional Paper  (A) Discrete Mathematics (B) Application of Mathematics In Finance and Insurance (C) Mathematical Modelling (D) Computational Mathematics Laboratory	50	
	Total	150	50

Total Marks - 150

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Subject Expert - Dr. Shabnam Khan
Subject Expert - Dr. S. K. Bhatt
Dr. Rakesh Tiwari
Dr. (Smt.) Prachi Singh
Dr. Shobha Rani

(1) Dr. Anil Kashyap (2) Shri A. K. Pandey (3) Dr. Mayur Puri Goswami -

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## **B.Sc. Part – III (MATHEMATICS)** 2022-2023 PAPER-I **ANALYSIS**

Max. Marks. 50

Course Title	se Title B. Sc. Part – III, Analysis	
CO No.	Course Outcomes - This course will enable the student to :	
CO No. – 1	Understand Series and their convergence, various test of convergent, Implicit function, Fourier series etc.	
CO No. – 2	Apply Reimman integration, mean value theorem, Integral as a function of parameter etc.	
CO No 3	Remember complex number, complex valued function, Analytic function, Conformal mapping etc.	
CO No 4	Understand Metric spaces, Contraction principle, Complete metric space, various types of spaces.	

#### METRIC SPACES:

- **UNIT-I** Construction of real numbers as the completion of the incomplete metric space of rationals. Real numbers as a complete ordered field. Definition and examples of metric spaces. Neighborhoods. Limit points. Interior points. Open and closed sets. Closure and interior. Boundary points. Sub-Space of a metric space. Cauchy sequences. Completeness. Cantor's intersection theorem. Contraction principle.
- **UNIT-II** Dense subsets. Baire Category theorem. Separable space, second countable and first countable spaces. Continuous functions. Extension theorem. Uniform continuity. Isometric and homeomorphism. Equivalent metrices. Compactness, Sequential compactness. Totally bounded spaces. Finite intersection property. Continuous functions and compact sets. Connectedness. Components. Continuous functions and connected sets.

#### COMPLEX ANALYSIS:

UNIT-III Complex numbers as ordered pair. Geometric representation of Complex numbers. Stereographic projection. Continuity and differentiability of complex functions. Analytic functions. Cauchy-Riemann equations. Harmonic functions. Elementary functions. Mapping by elementary functions. Mobius transformations. Fixed point. Cross ratio. Inverse points and critical mappings. Conformal mappings.

#### **REAL ANALYSIS:**

UNIT-IV Riemann integral. Integrability of continuous and monotonic functions. The fundamental Theorem of integral calculus. Mean value theorems of integral calculus. Improper integrals and their

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convergence, comparision tests, Abel's and Dirichlet's tests. Frullani's integral. Integral as a function of a parameter. Continuity, derivability and integrability of an integral of a function of a parameter.

UNIT-V Series of arbitrary terms. Convergence, divergence and oscillation. Abel's and Dirichlet's test.

Multiplication of series. Double series. Partial derivation and differentiability of real valued functions of two variables. Schwarz and Youngs theorem. Implicit function theorem. Fourier series. Fourier expansion of piece wise monotonic function

#### REFERENCES:

- 1. T.M. Apostol, Mathematical Analysis, Narosa Publishing House, New-Delhi, 1985.
- 2. R.R. Goldberg, Real Analysis, Oxford & IBH Publishing Company New-Delhi, 1970.
- 3. S. Lang, Undergraduate Analysis, Springer-Verlag, New-York, 1983
- 4. D.Somasunderam and B. Choudhary, A First Course in Mathematical Analysis, Narosa Publishing House, New Delhi,1997.
- 5. Shanti Narayan, A Course of Mathematical Analysis, S. Chand & Company New-Delhi.
- 6. P.K. Jain and S.K. Kaushik, An Introduction to Real Analysis, S. Chand & Company New-Delhi, 2000.
- 7. R.V. Churchill & J.W. Brown, Complex Variables and Applications, 5<sup>th</sup> Edition, Mc-Graw Hill, New-York, 1990.
- 8. Mark J. Ablowitz & A.S. Focas, Complex Variables: Introduction and Applications, Cambridge University Press South Asian Edition, 1998.
- 9. Shanti Narayan, Theory and Functions of a Complex Variable, S. Chand & Company New-Delhi. E.T. Copson. Metric Spaces Cambridge University Press, 1968.

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Dr. (Smt.) Prachi Singh

(Scheme of Autonomy)

## B.Sc. Part – III (MATHEMATICS)

#### 2022-2023

#### Paper II

#### **Abstract Algebra**

Max.Marks.50

Course Title	ourse Title B. Sc. Part – III, Abstract Algebra	
CO No.	Course Outcomes - This course will enable the student to :	
CO No 1	Understand Group Automorphism, Sylow's Theorems, Homomorphism of rings, Idea of Ideals, Euclidian rings, Modules etc	
CO No. – 2	Analyze Vector spaces and its property, Idea of dimension, dimension of sums of subspace.	
CO No 3	Evaluate Linear transformation with their matrix representation, Rank and nullity, digonalization, bilinear quadratic Hamilton's forms etc.	
CO No 4	Apply Inner product space, Orthogonal vectors, Gram Schmidt orthogonalization process etc.	

- UNIT-I Group Automorphism, inner automorphism. Automorphism groups. Conjugacy relation. Normalizer. Counting principle and the class equation of a finite group. Center for groups of prime order. Abelianizing of a group and its universal property. Sylow's theorems. Sylow subgroup. Structure theorem for finite abelian groups.
- UNIT-II Ring theory Ring homomorphism. Ideals and Quotient rings. Field of quotients of an integral domain. Euclidean rings. Polynomial rings. Polynomials over the rational field. Eisenstien criterion. Polynomial rings over commutative rings. Unique factorization domain. R-unique factorization domain implies so is R [x<sub>1</sub>,x<sub>2</sub>.....x<sub>n</sub>]. Modules, submodules. quotient modules. Homomorphism and isomorphism theorems.
- UNIT-III Definitions and examples of vector space. Subspaces. Sum and direct sum of subspaces. Linear span. Linear dependence, independence and their basic properties. Basis. Finite dimensional vector spaces. Existence theorem for basis. Invariance of the number of elements of a basis set. Dimension. Existence of complementary subspace of a finite dimensional vector space. Dimension of sums of subspaces. Quotient space and its dimension.
- UNIT-IV Linear transformation and their representation as matrices. The algebra of linear transformations. The rank-nullity theorem. Change of basis. Dual space, Bidual space and natural isomorphism. Adjoint of linear transformation. Eigen values and

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eigenvectors of a linear transformation. Diagonolisation, Annihilators of a subspace. Bilinear, Quadratic and Hermilton forms.

UNIT-V Inner product spaces - Cauchy-Schwarz inequality. Orthogonal vectors. Orthogonal complements. Orthogonal normal sets and basis. Bessel's inequality and for finite dimensional spaces. Gram-Schmidt orthogonalization process.

#### REFERENCES:

- 1. I.N.Herstien, Topics in Algebra, Wiley Eastern Ltd. New-Delhi.
- 2. N. Jacobson, Basic Algebra Vols. I & II, W.H. Freeman, 1980.
- 3. Shanti Narayan, A Text book of Modern Abstract Algebra, S. Chand & Company New-Delhi.
- 4. K.B. Dutta, Matrix and Linear Algebra , Prentice Hall of India Pvt. Ltd. New-Delhi 2000.
- 5. P.B.Bhattacharya, S.K.Jain and S.R.Nagpal, Basic Abstract (2<sup>nd</sup> edition) Cambridge Univercity Press, Indian edition, 1997.
- 6. K.Hoffman and R.Kunze, Linear Algebra 2<sup>nd</sup> Edition, Prentice Hall Englewood Cliffs, New Jersey. 1997.
- 7. S.K.Jain, A Gunawardena & P.B.Bhattacharya, Basic Linear Algebra with MATLAB. Key college publishing (Springer Verlag) 2001
- 8. S. Kumaresan, Linear Algebra, A Geeometric Approach, Prentice-Hall of India, 2000.
- 9. Vivek Sahai and vivkas bist, Algebra Norosa Publishing House, 1997.
- 10. I.S. Luther and B.S.Passsi, Algebra Vol. 1-Groups, Vol. II-Rings. Norosa Publishing House (Vol.1-1996, Vol.II-1999)
- 11. D.S. Malik, J.N.Mordeson and M.K.Sen Fundamentals of Abstract Algebra, McGraw Hill International Edition, 1997.

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# B.Sc. Part – III (MATHEMATICS) 2022-2023 Paper III Discrete Mathematics

Max.Marks.50

Course Title	Course Title B. Sc. Part – III, Discrete Mathematics	
CO No.	Course Outcomes - This course will enable the student to :	
CO No. – 1	Understand of discrete graphs, connected and strongly connected graphs etc.	
CO No. – 2	Analyze various graphs in which Eularian and Hamiltonian graph with special importance.	
CO No 3	Apply finite state machine and their application, Boolean algebra in switching circuits.	
CO No 4	Remember discrete numeric function its use in recurrence relation and generatic fuction.	

- UNIT -I Sets and proposition cardinality. Mathematical induction. Principle of inclusion and exclusion.
  Computability and formal languages Ordered sets. Languages, Phrase structure grammars.
  Types of grammars and languages. Permutations, Combinations and Discrete probability.
- UNIT -II Relations and Functions Binary relations, Equivalence relations and partitions. Partial order relation and lattices. Chains and anti chains. Pigeon hole principle. Graphs and planar graphs Basic terminology, Multi graphs, Weighed graphs, Paths and circuits, Shortest paths, Eularian paths and circuits. Travelling salesman problem, Planar graphs. Trees.
- UNIT -III Finite state machines Equivalent machines. Finite state machines as language recognizers.
  Analysis of algorithms Time complexity. Complexity of problems. Discrete numeric functions and Generating functions.
- UNIT IV Recurrence relations and Recursive algorithms Linear recurrence relations with constant coefficients. Homogeneous solutions. Particular solution. Total solution. Solution by the method of generating functions. Brief review of Groups and Rings.
- UNIT- V Boolean algebras Lattice and Algebraic structures. Duality. Distributive and Complemented Lattices. Boolean lattices and Boolean algebras. Boolean functions and Expressions. Propositional calculus. Design and implementation of Digital Networks. Switching circuits

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#### REFERENCES:

(1) C.L.Liu, Elements of Discrete Mathematics. [Second Edition], McGraw Hill, International edition, Computer Science series, 1986.

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## B.Sc. Part – III (MATHEMATICS) 2022-2023

#### Paper III (Optional)

## Application of Mathematics in Finance and Insurance

Max.Marks.50

#### Application of Mathematics in Finance:

- UNIT- I Financial Management An Overview- Nature and Scope of Financial Management, Goals of Financial Management and main decisions of Financial Management, Difference between risk, speculation and gambling. Time value of Money-Interest rate and discount rate, Present value and future value discrete case as well as continuous compounding case, Annuities and its kinds.
- UNIT- II Meaning of return, Return as Internal Rate of Return(IRR), Numerical Methods like Newton-Raphson Method to calculate IRR, Measurement of returns under uncertainty situations, Meaning of risk, Difference between risk and uncertainty, Types of risks, Measurement of risk, Calculation of security and Portfolio Risk and Return-Markowitz Model, Sharpe's Single Index Model Systematic Risk and Unsystematic Risk.
- UNIT-III Taylor Series and Bond Valuation, Calculation of Duration and Convexity of bonds, Financial Derivatives - Futures. Forward, Swaps and Options, Call and Put Option, Call and Put Parity Theorem, Pricing of contingent claims through Arbitrage and Arbitrage Theorem.

#### Application of Mathematics in Insurance:

- UNIT -IV Insurance Fundamentals -Insurance defined, Meaning of loss. Chances of loss, peril, hazard, and proximate cause in Insurance, Costs and benefits of insurance to the society and branches of insurance-life insurance and various types of general insurance, Insurable loss exposures feature of a loss that is ideal for insurance, Life Insurance Mathematics - Construction of Mortality Tables, Computation of Premium of Life Insurance for a fixed duration and for the whole life.
- Determination of clains for General Insurance-Using Poisson Distribution and Negative Binomial UNIT- V Distribution-the Polya Case Determination of the amount of claims in General Insurance-Compound Aggregate claim Model and its properties, and claims of reinsurance, Calculation of a compound claim density function, F-recursive and approximate formulae for F.

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#### REFERENCES:

- 1. Aswath Damodaran, Corporate Finance Theory and Practice, John Wiley & Son's Inc.
- 2. John C. Hull, Options, Futures and Other Derivatives, Prentice Hall of Indian Private Ltd.
- 3. Sheldon M. Ross, An Introduction to Mathematical Finance, Cambridge University Press.
- 4. Mark S. Dorfman, Introduction to Risk Management and Insurance, Prentice Hall, Englwood Cliffs, New Jersey.
- 5. C.D.Daykin, T. Pentikainen and M. Pesonen, Practical Risk Theory for Actuaries, Chapman & Hall.

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## B.Sc. Part III (MATHEMATICS) 2022-2023

## Paper III (Optional)

### MATHEMATICAL MODELLING

Max.Marks.50

- UNIT-I The process of applied mathematics. Setting up first order differential equations—Qualitative solution sketching, Difference and differential equation growth models.
- UNIT-II Single-species Population Models, Population growth-An age structure model, The spread of Technological Innovation.
- UNIT-III Higher order Linear Models- A model for the detection of Diabetes, Combat modes, Traffic Models
   Car-following models, Equilibrium speed distributions.
- UNIT-IV Nonlinear Population growth models, Prey-Predator models, Epidemic growth models, Modelsfrom political science Proportional representation-cumulative voting, comparison voting.
- UNIT-V Applications in Ecological and Environmental subject Areas- Urban waste water management planning

#### REFERENCES:

- 1. Differential Equation Models, Eds. Martin Braun, C.S. Coleman, D.A. Drew.
- 2. Political and Related Models, Steven J. Brams, W.F. Lucas, P.D. Straffin (Eds.)
- 3. Discrete and System models, W.F. Lucas, F.S. Roberts, R.M. Thrall.
- 4. Life Science Models, H.M. Roberts & M. Thompson.
- 5. All volumes published as modules in Applied Mathematics, Springer-Verlag, 1982.

6. Mathematical Modeling, J.N. Kapur, New Age International, New Delhi.

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## B.Sc. Part – III (MATHEMATICS) 2022-2023

#### Paper III (Optional)

## **Computational Mathematics Laboratory**

Max.Marks.50

The student expected to familiarize himself / herself with popular software for numerical computation and optimization. Real life problems requiring knowledge of numerical algorithms for linear and nonlinear algebraic equations, Eigen value problems, Finite difference methods, Interpolation, Differentiation, Integrations, Ordinary differential equations etc. should be attempted. Capabilities to deal with linear, integer and nonlinear optimization problems need to be developed. The objective of such a laboratory is to equip students to model and simulate large-scale systems using optimization modeling languages. (The concerned teacher is expected to provide the necessary theoretical background before the student does the corresponding practical). To this end software like MATLAB, LINDO, MATHEMATICA, MAPLE can be adopted. Following course outline is suggested based on MATLAB and LINDO.

- UNIT 1: Plotting of functions, Matrix operations, vector and matrix manipulations, matrix function, Data analysis and curve fitting.
- UNIT 2: Use of FFT algorithms, Numerical integrations.
- UNIT 3: Nonlinear equations and optimization functions, Differential equations.
- UNIT 4: 2-D Graphics and 3-D Graphics general purpose graphics functions, color maps and color controls, Examples: Number theory, picture of an FFT, Function of a complex variable, chaotic motion in 3-D.
- UNIT 5: Sparse matrices iterative methods for sparse linear equations, Eigen values of sparse matrices, Game of life, Linear programming, integer programming and Quadratic programming - modeling and simulation techniques.

11 Ren.

#### **REFERENCES:**

- 1. MATLAB High performance numeric computation visualization software: Users guide.
- 2. MATHEMATICA Stephen Wilfram, Cambridge.
- 3. Introduction to operations research, F. S. Hiller and G. J. Lieberman.
- 4. Optimization modeling with LINDO: Linus Schrage.

Chairperson / H.O.D - Dr. M.A. Siddiqui

Subject Expert - Dr. Madhu Srivastava

Subject Expert - Dr. Shabnam Khan

Subject Expert - Dr. S. K. Bhatt

Representative Members -

(1) Dr. Anil Kashyap -

(2) Shri A. K. Pandey -

(3) Dr. Mayur Puri Goswami -

Faculty members -

Dr. Padmavati

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Dr. (Smt.) Prachi Singh